

Rational Root Theorem Day 2 HW

Name \_\_\_\_\_

For each problem:

- a) List the possible rational roots (p's/q's)
- b) Factor completely (hint: Use synthetic to get you started!)
- c) List all real zeros
- d) Graph making note of the x-intercept(s) and y-intercept

1.  $s(x) = x^3 + 4x^2 + 5x + 2$

2.  $b(x) = 5x^3 + 29x^2 + 19x - 5$

3.  $c(x) = x^4 - 12x^3 + 42x^2 - 52x + 21$

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1.  $s(x) = x^3 + 4x^2 + 5x + 2$

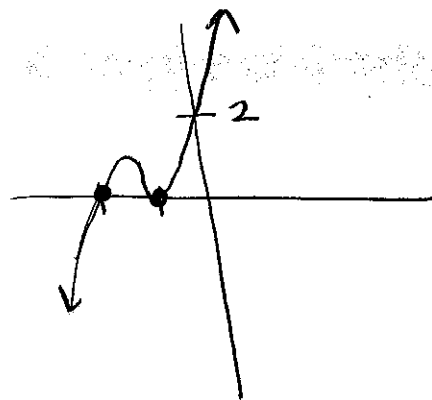
a)  $\frac{\pm 1 \pm 2}{\pm 1 \pm 2}$

b) 
$$\begin{array}{r|rrrr} -1 & 1 & 4 & 5 & 2 \\ & & -1 & -3 & -2 \\ \hline & 1 & 3 & 2 & 0 \end{array}$$

$(x+1)(x^2+3x+2)$   
 $(x+1)(x+2)(x+1)$   
 $(x+2)(x+1)^2$

c)  $x = -2, -1^*$

deg = 3 ✓ ↑



2.  $b(x) = 5x^3 + 29x^2 + 19x - 5$

a)  $\frac{\pm 1 \pm 5}{\pm 5 \pm 1/5 \pm 5/5 = 1}$

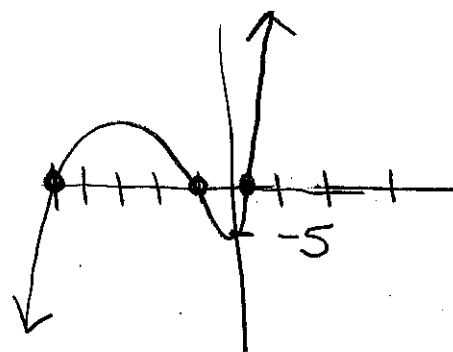
b) 
$$\begin{array}{r|rrrr} -1 & 5 & 29 & 19 & -5 \\ & & -5 & -24 & 5 \\ \hline & 5 & 24 & -5 & 0 \end{array}$$

$(x+1)(5x^2+24x-5)$   
 $(x+1)(x+5)(5x-1)$

MFDG  
 $x^2+24x-25$   
 $(x+\frac{25}{5})(x-\frac{1}{5})$   
 $(x+5)(5x-1)$

c)  $x = -1, -5, 1/5$

deg = 3 ✓ ↑



3.  $c(x) = x^4 - 12x^3 + 42x^2 - 52x + 21$

a)  $\frac{\pm 1 \pm 3 \pm 7 \pm 21}{\pm 1 \pm 3 \pm 7 \pm 21}$

b) 
$$\begin{array}{r|rrrrr} 1 & 1 & -12 & 42 & -52 & 21 \\ & & 1 & -11 & 31 & -21 \\ \hline & 1 & -11 & 31 & -21 & 0 \end{array}$$

$(x-1)(x^3-11x^2+31x-21)$

c) x-int =  $1^*, 3, 7$

$$\begin{array}{r|rrrr} 1 & 1 & -11 & 31 & -21 \\ & & 1 & -10 & 21 \\ \hline & 1 & -10 & 21 & 0 \end{array}$$

$(x-1)(x-1)(x^2-10x+21)$   
 $(x-1)^2(x-3)(x-7)$

deg = 4 ✓ ↑

